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On Possible Glueball Nature of Soft Pomeron^{*}

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Abstract: We study the gluonic content of the Pomeron through relating the Pomeron trajectory to the observed $I^G J^{PC} = 0^+ 2^{++}$ isoscalar tensor mesons. Four of these mesons satisfy the spin-mass relation of the Pomeron. These Pomeronian candidates may be hybrid states. One of them, the $f_2(2220)$ meson, can have a predominant glueball component. We address the unsettled experimental situation about the width of this meson and give a theoretical lower bound for it. We also show why this meson has not been seen in $\bar{p}p$ experiments.

Key words : Pomeron; glueball; meson

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1 Introduction

Before the advent of the quantum chromodynamics (QCD) field theory, Regge theory was successfully used in describing and predicting hadron-hadron elastic scattering and diffractive dissociation^[1, 2]. Although Regge theory is not a field theory, it is based upon a set of postulates (or axioms) about the S -matrix, which is believed to govern the strong interaction physics. Consequently, the Regge theory can not be completely disconnected from QCD. In Regge theory, mesons and baryons are organized into families of trajectory (the Regge trajectories or Reggeons) which play an important role in hadronic dynamics. The most tantalizing prediction of the theory is that when the interaction energy becomes very large only one trajectory contributes to hadron-hadron elastic scattering. This unique trajectory is called the Pomeron

trajectory or Pomeron, named in honor of physicist Pomeranchuk^[3]. The members of the Pomeron trajectory all have the quantum numbers of a vacuum except their spins.

Although no particles that fit the Pomeron properties were observed during the heyday of the Regge theory, many new particles have since been discovered thanks to a new generation of accelerators. Some of these particles may be the glueballs predicted only by the QCD theory. As a result of this progress, there is a surge of interests in understanding the success of the Regge theory through connecting glueballs with the Pomeron. Because glueballs are bound states of the gluons, they can only be understood in terms of non-perturbative QCD. An establishment of the Pomeron-Glueball link could aid our understanding of non-perturbative QCD.

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The Pomeron is a successful mediator in describing high energy strong interaction diffractive processes, such as pp , $\bar{p}p$, and $\gamma^* p \rightarrow Vp$ with V being the vector mesons ω , ρ , J/ψ , ϕ and ν . However, the gluonic origin and particle nature of the Pomeron are still unknown at present. No known particle lies on the Pomeron trajectory. Most current studies of Pomeron physics are in conventional level in which people analyse the Pomeron coupling to the nucleon and derive the intercept $\alpha_P(0)$ and slope α'_P of the Pomeron trajectory $\alpha_P(t) = \alpha_P(0) + \alpha'_P t$. Namely, they are phenomenological studies. In this paper we investigate the Pomeron physics using the fundamental theory of strong interaction QCD and initially study the gluonic origin and tensor glueball nature of the Pomeron. We point out the Pomeron could be a tensor glueball with mass of 2.23 GeV, decay width of $\Gamma_\xi \simeq 100$ MeV and quantum numbers $I^G J^{PC} = 0^+ 2^{++}$. This is a very important point of our present paper. According to our best knowledge, we have not found, so far, any other publications in literature which has proposed the same idea as ours.

The paper is organized as follows: In section 2, we recapitulate the main results of the Regge theory on the Pomeron. In section 3, we discuss the gluonic content of the Pomeron. We show in section 4 the connection between the Pomeron and tensor mesons with a focus on the $f_2(2220)/\xi$ meson because of the reported flavor-symmetry decay and the unsettled experimental situation. We give a lower bound for the width of ξ , with which the seemingly opposing results given by different experiments can be explained. The conclusions are given in section 5.

2 Regge Theory and Pomeron

Unlike QCD field theory, the Regge theory does not involve gauge particles. Instead, it explores the consequences of a set of fundamental postulates of the S-matrix; in particular, the Lorentz invariance, the unitarity, and the analytic-

ity of the S-matrix. The Regge theory was motivated by the experimental observation that at high energies the hadron-hadron (hh) elastic scattering and diffractive dissociation are mainly diffractive. Because exchanging a particle in t-channel will give rise to a forward-peaking, diffractive amplitude in the s-channel, the Regge theory conjectures that the high-energy hadronic dynamics is driven by t-channel exchanges.

There is, however, an important difference between the Regge theory and the meson-exchange model used in medium-energy physics. It can be shown that the exchange of a particle of spin J in the t-channel will necessarily lead to a total cross section $\sigma^{\text{tot}}(s) \approx s^{J-1}$, which diverges with s for $J > 1$. Hence, simple particle-exchange models will lead to divergent energy-dependent cross sections, which have to be cured by introducing ad-hoc energy-cutoff form factors. Regge theory overcame this difficulty by not using particle exchanges but by using trajectory exchanges with each trajectory carrying a running spin $\alpha(t)$, which is a complex-valued function of the exchanged 4-momentum t . The connection of a Regge trajectory, $\alpha(t)$, to a physical particle having mass m and spin J is that $J = \text{Re}[\alpha(t=m^2)]$. In other words, a Regge trajectory or a Reggeon is a family of reggeized particles constrained on a spin trajectory $\alpha(t)$.

As a result of trajectory exchange, the Regge theory gives $\sigma^{\text{tot}} \approx s^{\alpha(0)-1}$. Because all the trajectories associated with the known particles^[2] have $\alpha(0) < 1$, the cross section no longer diverges. In fact, this last inequality implies that the contribution of a given trajectory will die off at very high energies. However, experimental total cross sections do not vanish asymptotically^[4]. Instead, they rise slowly as s increases. The high-energy total cross sections of the pp , $\bar{p}p$, $\pi^+ p$, $\pi^- p$ reactions are found to follow the energy dependence^[5]

$$\sigma_{\text{tot}} = As^{0.0808} + Bs^{-0.4525} \text{ (mb)}, \quad (1)$$

where A and B are constants. The appearance of a

universal exponent 0.080 8 indicates unequivocally that if one attributes this mild rise of the cross sections to the exchange of a single Regge trajectory, then this trajectory has $\alpha(0) \simeq 1.08$.

The s -dependence of the cross sections is shown in Fig. 1 where at high energies $\sigma(\text{pp}) = \sigma(\bar{\text{p}}\bar{\text{p}})$ and $\sigma(\pi^+ \text{p}) = \sigma(\pi^- \text{p})$. The equality $\sigma(\text{hp}) = \sigma(\bar{\text{h}}\bar{\text{p}})$ at very high energies was foreseen by Pommeranchuk^[3]. In order to account for it, this Regge trajectory must carry the quantum numbers of vacuum, except its spins. In other words, it has $B = Q = S = I = 0$ and $P = G = C = +$ but with spin J given by $\alpha(t)$. This unique trajectory was named the Pomeron trajectory (or Pomeron).

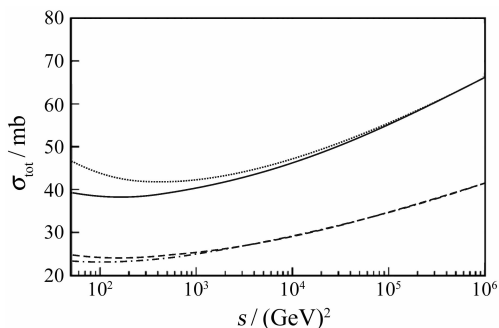


Fig. 1 The s -dependence of the total cross sections for various reactions.

The top two curves denote pp and $\bar{\text{p}}\bar{\text{p}}$ elastic scattering while the low two curves stand for $\pi^+ \text{p}$ and $\pi^- \text{p}$ elastic scattering.

Although the Regge trajectory $\alpha(t)$ can be a nonlinear function of t , it can be well approximated by a linear function at low t 's. For the purpose of studying the Pomeron, it suffices to use the form

$$\alpha(t) = 1.08 + \alpha' t. \quad (2)$$

In contrary to $\alpha(0)$, the value of the slope α' is less unanimous. The most extensively quoted value of $\alpha' = 0.25 \pm 0.02$ was first given in Ref. [6], resulted from fitting the slope of the pp elastic differential cross sections at small momentum transfers. There are two other methods that have been used

for determining the α' . One method used an effective trajectory approach ($\xi 6.8e$ of Ref. [2]) which gave* an $\alpha' = 0.20 \pm 0.01$. The other^[7] used the relation** $\sigma_{\text{tot}}^2(s)/\sigma_{\text{el}}(s) = 16\pi(b + 2\alpha' \ln(s))$, with b being the slope of the experimental elastic diffraction peak. The pp total and elastic cross sections then gave^[7] an $\alpha' = 0.20 \pm 0.02$. Hence, the last two methods gave the same result.

One should note, however, that the analysis of Ref. [6] that led to $\alpha' = 0.25$ is model-dependent. More precisely, the theoretical formula employed for fitting the data was based on a phenomenological quark model and on valence quark counting rule. Consequently, it is not possible to know the systematic uncertainty of the α' , arising from using such a theoretical model. In contrast, the methods of Refs. [2] and [7] are model independent. In particular, in spite of the use of very different data sets, these two different methods gave the same α' . For this reason, the value of $\alpha' = 0.20$ should be chosen.

In Fig. 2 we plot the Pomeron trajectory zone defined by different values of α' . We also plot, in ascending mass order, the isoscalar tensor resonances $f_2'(1525)$, $f_2(1565)$, $f_2(1640)$, $f_2(1810)$, $f_2(1950)$, $f_2(2010)$, $f_2(2150)$, $f_2(2220)$, $f_2(2300)$, $f_2(2340)$. As we can see, the $f_2(2010)$, $f_2(2150)$, $f_2(2220)$ are inside the zone bordered by the solid lines. The $f_2(1950)$ is marginal because it is inside the zone only when the higher value of 0.25 (the chain-dotted line) is used.

To this end, we caution that in the literature two kinds of Pomerons, hard and soft, have been discussed. The hard Pomeron is associated with large momentum transfer. Recent experimental data on large rapidity gap events at HERA^[8] gave some evidence for the existence of large Q^2 , hard

* The uncertainties were not given in the original articles and are the results of refitting the same inputs by us.

** More precisely, the relation is $\sigma_{\text{tot}}^2(s)/\sigma_{\text{el}}(s) = 16\pi(b + 2\alpha' \ln(s))/(1 + \rho^2)$ with ρ being the ratio of the real to imaginary parts of the forward amplitude. However, in the energy region of interest, $(\rho^2 + 1) \simeq 1$.

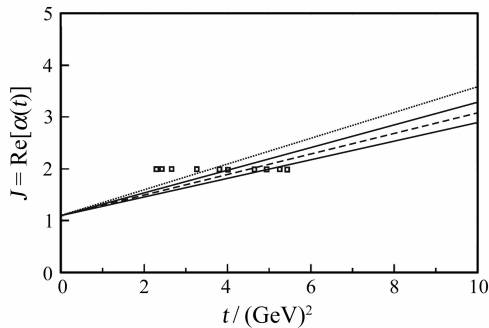


Fig. 2 Zone of the Pomeron trajectory.

The threshold of $p\bar{p}$ is at $t = 3.25 (\text{GeV})^2$ where the open squares stand for 10 isoscalar tensor resonances as we discussed in Sect. 2.

Pomeron. It is not the original or the soft Pomeron conjectured in Regge theory; the latter is associated with small Q^2 . The four tensor resonances mentioned in the previous paragraph are, therefore, the candidates for the soft Pomeron. In terms of QCD, the hard Pomeron is in the perturbative (pQCD) regime while the soft Pomeron must be studied with non-perturbative method. The evolution from the hard to soft Pomeron or vice versa is still an unresolved problem. There are many studies of diffractive processes using hard or semi-hard Pomeron models^[5, 9]. We shall not discuss these models and will concentrate on the soft Pomeron.

3 Gluonic Content of the Pomeron

In QCD, the simplest model for vacuum exchange with properties similar to that of the Pomeron is two interacting gluons. This was emphasized by Nachtmann^[10], who stated that the two-gluon system has all the properties that a Pomeron should possess. The idea of modelling the Pomeron with two gluons was originated by Low^[11]. The model was further developed by Nussinov^[12] who considered more than two gluons. Subsequent and more sophisticated considerations led to the development of BKFL^[13] and DGLAP^[14] equations. All these models use pQCD and all gave an $\alpha(0) \gg 1$. These studies indicate, therefore, that models involving gluons but not bound gluons can-

not describe the soft Pomeron. Consequently, if gluons are the constituents of the soft Pomeron, they must be in a bound state.

The existence of bound states of gluons (the glueballs) is a consequence of self-coupling of gluons in QCD. Lattice calculations and other theoretical models^[15, 16] have predicted that the lightest glueballs have $J^{PC} = 0^{++}$ (scalar glueball) and 2^{++} (tensor glueball).

Although scalar glueballs have been studied extensively^[17, 18], they cannot be the soft Pomeron because spin = 0 is ruled out by Eq. (2). Moreover, Levin noted^[19] that the process due to exchanging scalar particle is not diffractive and becomes less important as energy increases. From the discussion given after Eq. (2), the lightest soft Pomeron must have spin $J=2$. Fig. 2 indicates that four $J=2$ isoscalar tensor resonances in the 2 GeV mass region are compatible with the Pomeron trajectory. Can one of them be a tensor glueball?

Calculated glueball spectra predict^[15, 16, 20] that the lightest 2^{++} tensor glueball has a mass about $(2.2 \pm 0.3) \text{ GeV}$. Because in lattice calculations the quark masses are taken to be infinite and the $q\bar{q}$ loops are neglected, the mixing of $q\bar{q}$ and glueball states can not occur in those calculations. However, the existence of a 2^{++} tensor glueball in the 2 GeV mass region is also predicted by other theoretical models^[21, 22]. In addition, a mass-equation analysis of all the observed isoscalar tensor states has indicated^[23] that while $f_2'(1525)$ and $f_2(1640)$ are definitely quarkoniums, the tensor states of larger masses can be $q\bar{q}$ -gluons hybrids. The mass equation also has a solution corresponding to $f_2(2220)$ being almost a tensor glueball.

In summary, the soft Pomeron can not be unbound gluons or scalar glueballs. The pomeronian candidates have $I^G(J^{PC}) = 0^+(2^{++})$ and a mass in the 2 GeV region. Some analyses suggest that they are hybrid states and one of them, the $f_2(2220)$, may be a tensor glueball.

4 $f_2(2\ 220)/\xi$ Meson

In 1986 the MARK III collaboration^[24] at SLAC observed a narrow resonance, named ξ , in the decay of J/ψ to $K_S K_S$ and $K^+ K^-$ channels. It was reported that $M_\xi = (2\ 230 \pm 15)$ MeV and $\Gamma_\xi = (18_{-15}^{23} \pm 10)$ and $(26_{-16}^{+26} \pm 7)$ MeV respectively, and that $J^{PC} = (\text{even})^{++}$. At the same time, Alde *et al.* also observed^[25] a broad enhancement ($\Gamma \ll 150$ MeV) at $M=2\ 220$ MeV in the reaction $\pi^- p \rightarrow nX$, $X \rightarrow \eta\eta'$. The ξ was also seen^[26] in $K_S^0 K_S^0$ and in the WA91 collaboration^[27] at CERN. However, it was not seen in γ decays and in inclusive B decays. In 1996, BES collaboration^[28] reported the observation of $\xi(2\ 230)$ in the radiative decay of the J/ψ to $\bar{p}p$, $K^+ K^-$, $K_S^0 K_S^0$, $\pi^+ \pi^-$ channels. The data also suggest a spin $J=2$ or 4. However, the $\xi(2\ 230)$ was not seen in experiments^[29] $\bar{p}p \rightarrow K^+ K^-$, $K_S K_S$, $\phi\phi$, $\pi^+ \pi^-$. In our opinion, these seemingly contradictory experimental results do not necessarily rule out the existence of ξ . We will come back to this point toward the end of this section. In the following discussion we will use interchangeably the notations $f_2(2\ 220)$ and ξ .

Because the BES collaboration observed ξ in the $J/\psi \rightarrow \gamma\xi$; $\xi \rightarrow \bar{p}p$ reaction and because the $\bar{p}p$ channel is related to the pp channel by crossing symmetry, it is of value to investigate contributions by ξ to high-energy pp scattering in the framework of Regge theory. In particular, because pp elastic scattering is a diffractive process^[30] in which no quantum numbers are exchanged between the colliding particles, it is an ideal place for inves-

tigating the Pomeron. If the Regge-exchange of a tensor meson can describe the observed pp elastic scattering as does the Pomeron, then it would be a strong indication that meson is a Pomeron.

We have carried out such analysis in Ref. [31]. The original analysis was done for the ξ , we now extend it to all f_2 mesons of interest. Although the Regge analysis alone is not sufficient to uniquely determine which tensor state is the Pomeron, as we shall see, it gives a definite prediction on the partial decay width $\Gamma_{f_2 \rightarrow p\bar{p}}$ which can be used to analyze experiments to pin down the Pomeron. Once the identification of the tensor meson to the Pomeron is achieved, the gluonic content of that meson will be the gluonic content of the Pomeron.

The results obtained from applying the theory to fitting simultaneously the pp total cross section and to the diffraction peak of the pp elastic differential cross sections are summarized in Table 1. The form factor ranges (λ_s , λ_t) and the coupling constants (\bar{g}_1 , \bar{g}_3) are result of the fit. On the other hand, the partial decay widths $\Gamma_{f_2 \rightarrow p\bar{p}}$ are theoretical predictions based on the fit (see Appendix).

As mentioned at the beginning of this section, there are currently opposing experimental results about the existence of the $f_2(2\ 220)/\xi$ meson. In particular, this resonance was not seen in the $\bar{p}p$ experiments, which seems to contradict the results reported in Ref. [28]. We believe that the partial decay width given by our analysis can shed lights on how to understand the unsettled experimental situation.

Table 1 Predicted partial decay widths to the $\bar{p}p$ channel from the pp scattering at $\sqrt{s} = 53$ and 62 GeV

Mesons	\sqrt{s}/GeV	λ_s/GeV	λ_t/GeV	g_1	g_3	$\Gamma_{f_2 \rightarrow p\bar{p}}/\text{MeV}$
$f_2(2\ 220)/\xi$	53	0.65 — 0.67	3.79 — 3.82	1.70 — 1.72	0.00 — 0.02	1.94 — 1.99
	62	0.66 — 0.68	3.74 — 3.79	1.67 — 1.70	0.00 — 0.01	1.88 — 1.94
$f_2(2\ 150)$	53	0.66	3.88 — 3.99	1.53 — 1.56	0.00 — 0.04	1.49 — 1.53
	62	0.67	3.89 — 3.96	1.49 — 1.55	0.00 — 0.05	1.41 — 1.53
$f_2(2\ 010)$	53	0.66 — 0.67	3.42 — 4.35	1.04 — 1.18	0.00	0.54 — 0.70
	62	0.67	3.94 — 4.18	1.12 — 1.15	0.00	0.62 — 0.65

(a) We see from Table 1 that the partial decay widths of all the f_2 mesons are extremely narrow. Furthermore, $g_3 \ll g_1$, indicating the f-wave ($L=3$) component of the vertex is negligible. Both are the consequence of the fact that the masses of these mesons are very close to the $p\bar{p}$ threshold. The narrowness of the partial width indicates that the $p\bar{p}$ decay channel must be a small part of the total decay of these f_2 mesons.

(b) The BES collaboration reported similar branching ratios (BR) for $\xi \rightarrow p\bar{p}, K^+K^-, K_S^0K_S^0, \pi^+\pi^-$ decay modes. In subsequent publications^[32, 33] the BES collaboration reported the observation of $\xi \rightarrow \pi^0\pi^0, \eta\eta, \eta\eta', \eta'\eta'$. It is indicated that the BR for $\pi^0\pi^0$ is similar to that for $\pi^+\pi^-$. However, in Ref. [32] the width Γ_ξ^{tot} was not given by the analysis but was prefixed at 20 MeV. As to the BR for $\eta\eta, \eta\eta', \eta'\eta'$, a much higher upper bound was given^[33]. Assuming equal BRs for all these 8 decay modes and taking from Table 1 the average value of $\Gamma_{\xi \rightarrow p\bar{p}} = 1.94$ MeV, we obtain a $\Gamma_\xi^{\text{tot}} \simeq 16$ MeV. Taking into account the experimental uncertainties of the widths given in Ref. [28], this 16 MeV width represents already the observed value, implying there are no other decay modes left unobserved. This is a very unlikely possibility.

It was also reported in Ref. [28] that the BR of ξ decaying into $\pi^+\pi^-$ is equal to or less than 2%. Assuming again equal BR, then the 2%-fraction and $\Gamma_{\xi \rightarrow p\bar{p}} = 1.94$ MeV imply that $\Gamma_\xi^{\text{tot}} = 1.94/0.02 = 97$ MeV which is very large compared with the value of ~ 20 MeV given in Ref. [28]. In order to obtain 20 MeV, the 2%-fraction would require the predicted $\Gamma_{\xi \rightarrow p\bar{p}}$ to be reduced by a factor of 5, i. e., reducing the coupling constant \bar{g}_1 by a factor of $\sqrt{5}$. We could not find such a solution in our analysis. Referring to Fig. 1, one can see that at $s = 2800$ to 3600 (GeV)², the Pomeron exchange is already a good description of the data. This led us to believe that the uncertainty of the prediction, as could arise from assuming the Pomeron exchange

alone, cannot be as big as a factor of five. Consequently, we believe that the currently reported $\Gamma_\xi^{\text{tot}} = (22 \pm 8)$ MeV^[4] is most likely an underestimate.

(c) A broad width is also consistent with the non-observation of a resonance structure in the 2.23 GeV region in the $p\bar{p}$ experiments^[29]. We recall that there are many broad resonances in the neighborhood of 2.23 GeV. Consequently, to $p\bar{p}$ reaction cross section is given by

$$\left(\frac{d\sigma}{dt}\right)_{a'a} = \left| \sum_j \frac{c_{a'ij}c_{jia}f(t)}{s - M_j^2 + iM_j\Gamma_j^{\text{tot}}} \right|^2, \quad (3)$$

where s and t are the total energy and the momentum transfer, $f(t)$ is the t -dependence of the differential cross section. The indices a and a' denote, respectively, the initial ($p\bar{p}$) and the final ($\bar{h}h$) channels, with $c_{jia} \propto \Gamma_j^{1/2} c_a$ and $c_{a'ij} \propto \Gamma_j^{1/2} c_{a'}$ being the coupling of the initial and final states to the resonance j . Clearly, a resonance structure will not show up in the energy dependence of the cross section if $c_{jia} = 0$, i. e., if the resonance j does not exist. However, we advocate that even if the resonance does exist the structure may still not be seen in the data.

We have examined the general feature of the energy dependence of the $p\bar{p} \rightarrow \bar{h}h$ reaction by firstly considering the case where only one single resonance, the $f_2(2220)/\xi$, contributes. Our calculations have shown that the shape of this energy dependence is very sensitive to the value of the Γ_ξ^{tot} . A resonance peak can be clearly seen in the mass region 2200 to 2500 MeV when Γ_ξ^{tot} is narrower than 50 MeV. However, the peak is no longer significant when Γ_ξ^{tot} is 75 MeV, and disappears when Γ_ξ^{tot} reaches ~ 100 MeV. This last value is in line with the 97 MeV mentioned in (b). We have also noted that including other resonances in the calculation led to a further reduction of the peak-to-background ratio but left the above main feature unaltered.

The $p\bar{p}$ experiment of Ref. [29] only scanned the mass region 2222.7 to 2239.7 MeV. Conse-

quently, that experiment can only confirm the existence of a narrow $f_2(2\ 220)/\xi$ resonance. In other words, a non-observation of the resonance structure is not a sufficient ground for rejecting the existence of ξ , as it may just indicate that ξ has a broad width. Our analysis puts, therefore, a lower bound of about 100 MeV for $\Gamma_{\xi}^{\text{tot}}$.

(d) It is generally accepted that the total decay width of a tensor glueball is narrow. However, current theoretical methods are still incapable of giving a quantitative statement about this narrowness. It is unclear whether 100 MeV is too broad for a glueball.

5 Conclusions

The lightest particle that can be the soft Pomeron must have a spin of 2 and a mass in the 2.2 GeV region. Three isoscalar tensor mesons, $f_2(2\ 010)$, $f_2(2\ 150)$, and $f_2(2\ 220)/\xi$, fit this requirement. Regge analysis can predict the $f_2 \rightarrow \bar{p}p$ partial decay width which, when used in combination with the experimental branching ratios, can determine the total decay width of the meson. Comparison between the theoretical and experimental total widths will pin down the Pomeron.

There is a great deal of interest in the $f_J(2\ 220)/\xi$ meson because the reported^[28] flavor-symmetry decay and narrow width of this meson fit what one expects from a glueball decay. However, the experimental situation is far from being settled. In particular, the ξ was not seen in the $\bar{p}p \rightarrow \pi^0\pi^0, \eta\eta$ experiments. Our interest in the ξ is related to the search for Pomeron, as this meson, with spin 2, is situated on the Pomeron trajectory (cf. Fig. 1). Our analysis has shown that the ξ must have a width much broader than the reported 22 MeV. A broader width does not necessarily rule out the ξ as a glueball, but it does explain why the meson cannot be seen in the $\bar{p}p$ experiments.

We have noted there are other tensor states that satisfy the Pomeron trajectory, among others, the $f_2(2\ 150)$ and $f_2(2\ 010)$ mesons. However,

good experimental information about their decay to the $\bar{p}p$ channel is sparse. Better information on the branching ratios of their various decay modes will allow analysis to be carried out at the same level as for the ξ .

If the spin of $f_J(2\ 220)/\xi$ is confirmed to be 2 and if the improved measurement gives a width compatible with what has been inferred from our Pomeron analysis, then the ξ can be identified with the Pomeron. In this case, the Pomeron will be a tensor glueball or at least have a dominant tensor glueball component. It is, however, still of great interest to carry out more detailed experimental studies of the $f_2(2\ 150)$ and $f_2(2\ 010)$ mesons as well as more refined theoretical studies on the gluonic content of their wave functions. By comparing the decay branching ratios of these two mesons with those of the ξ , one would better understand the Pomeron.

Finally, we note that other diffractive processes where the Pomeron exchange is believed to be dominant, such as diffractive dissociation of hadrons, electro-production of vector mesons from the proton, virtual Compton scattering, etc., should also be used to improve our understanding of the soft Pomeron and tensor states.

6 Appendix

We recapitulate the key results of Ref. [31]. The standard definition of the Mandelstam variables, helicities, and residue functions are employed. The t-channel Regge amplitude in the helicity basis^[34] is:

$$C_I \frac{A_{\lambda_2\lambda_1, i\lambda_1\lambda_3}^{(I)}(\bar{s}, \bar{t}) - 4\pi^2(2\alpha + 1)\beta_{\lambda\lambda'}(t)(-1)^{\alpha+\lambda} \frac{1}{2}[1 + (-1)^\alpha]}{\sin\pi(\alpha + \lambda')} \times d_{\lambda\lambda'}^{\alpha}(z_i), \quad (4)$$

where $C_I = 1/2$, $\bar{s} = t$, $\bar{t} = s$. The $\beta_{\lambda\lambda'}(t) \equiv \beta_{\lambda_2\lambda_1, i\lambda_1\lambda_3}(\bar{s})$ is the Regge residue. The λ_i is the helicity of the particle i , and $\alpha \equiv \alpha(t)$ is the trajectory spin. In Eq. (4), we have introduced for clarity the

variables \bar{s} and \bar{t} which denote, respectively, the total c. m. energy and the momentum transfer in the t-channel.

On the other hand, the Feynman amplitude due to exchanging a meson of spin J_2 is

$$A_{\lambda_{\bar{2}}\lambda_4; \lambda_1\lambda_{\bar{3}}}^{(\prime)}(t, s) = -4 M_{f_2}^2 \frac{4\pi(2J_2+1)}{2} \times \langle \lambda_{\bar{2}}\lambda_4 | \mathcal{M}^{J_2}(t) | \lambda_1\lambda_{\bar{3}} \rangle d_{\lambda_{\bar{2}}\lambda_4}^{J_2}(\alpha), \quad (5)$$

with

$$\begin{aligned} & \langle \lambda_{\bar{2}}\lambda_4 | \mathcal{M}^{J_2}(t) | \lambda_1\lambda_{\bar{3}} \rangle \\ &= \frac{G_{\lambda'} H_{\lambda_{\bar{2}}\lambda_4}^{J_2}(t) G_{\lambda} H_{\lambda_1\lambda_{\bar{3}}}^{J_2}(t)}{t - M_{f_2}^2 + i M_{f_2} \Gamma_{f_2}^{\text{tot}}}. \end{aligned} \quad (6)$$

In Eq. (6), $J_2=2$, $\lambda \equiv \lambda_1 - \lambda_{\bar{3}}$, and $\lambda' \equiv \lambda_{\bar{2}} - \lambda_4$. The $H(t)$ denotes the form factor of the $\text{pp}\bar{f}_2$ vertex in the helicity basis with G being the coupling constant, and M_{f_2} , $\Gamma_{f_2}^{\text{tot}}$, respectively, the mass and the full(total) decay width of the f_2 meson.

The reggeization of f_2 -exchange was realized through projecting the discrete spin value J_2 onto the continuous spin value α of the Regge trajectory and the result is^[31]

$$\beta_{\lambda\lambda'}(t) = -\alpha_R' 4M_p^2 G_{\lambda'} H_{\lambda_{\bar{2}}-\lambda_4; J_2}(t) G_{\lambda} H_{J_2; \lambda_1\lambda_{\bar{3}}}(t), \quad (7)$$

where $\alpha'_R \equiv \text{Re}[\alpha']$. Eq. (7) gives a Feynman description of the residue factorization used extensively in the Regge theory, which also answers why we started with the t-channel amplitude. We may also notice that the factorization of the Regge residue β is achieved at the same time of the reggeization.

The GH is directly related to the partial decay width $\Gamma_{f_2 \rightarrow \text{p}\bar{\text{p}}}$ through^[35]

$$\begin{aligned} & \frac{1}{2} \Gamma_{f_2 \rightarrow \text{p}\bar{\text{p}}} = \text{Im} [\Pi_{f_2}(t)] \\ &= C_I \frac{M_p^2}{M_{f_2}^2} \frac{|\mathbf{q}_r|}{16\pi^2} \sum_{\lambda_p\lambda_{\bar{p}}} |G_{\lambda} H_{\lambda_p\lambda_{\bar{p}}; J_2}(q_r^2)|^2, \end{aligned} \quad (8)$$

where $\mathbf{q}_r^2 \equiv t_r/4 - M_p^2 \equiv M_{f_2}^2/4 - M_p^2$ and $\lambda = \lambda_p - \lambda_{\bar{p}}$. The \mathbf{q}_r is the on-shell $\text{pp}\bar{f}_2$ relative momentum in the c. m. of the meson. Eq. (8) shows that the vertex GH can be obtained from calculating the self-energy $\Pi_{f_2}(t)$ of the tensor state. Conversely,

one can determine GH from pp scattering and to use it to predict $\Gamma_{f_2 \rightarrow \text{p}\bar{\text{p}}}$.

The s-channel amplitude is obtained through crossing-symmetry which reads

$$A_{(\text{pp} \rightarrow \text{pp}) \lambda_3\lambda_4; \lambda_1\lambda_2}^{(s)} = \mathcal{U}_{\lambda_3\lambda_4\lambda_1\lambda_2; \lambda'_{\bar{2}}\lambda'_4; \lambda'_1\lambda'_{\bar{3}}} A_{(\text{pp} \rightarrow \text{p}\bar{\text{p}}) \lambda'_{\bar{2}}\lambda'_4; \lambda'_1\lambda'_{\bar{3}}}^{(t)}. \quad (9)$$

Since there are five independent helicity amplitudes, \mathcal{U} is a 5×5 unitary matrix^[36]. The cross sections are given by^[31]

$$\begin{aligned} \sigma_{\text{tot}}^{\text{pp}} &= \frac{1}{2s} \sum_{\lambda_3\lambda_4; \lambda_1\lambda_2} \text{Im} [\mathcal{A}_{\lambda_3\lambda_4; \lambda_1\lambda_2}^{(s)}] |_{t=0} \\ &= \frac{1}{2s} \text{Im} [4\mathcal{A}_1^{(t)} + 8\mathcal{A}_5^{(t)}] |_{t=0}, \end{aligned} \quad (10)$$

and

$$\begin{aligned} \frac{d\sigma^{\text{pp}}}{dt} &= \frac{1}{16\pi s^2} \sum_{\lambda_3\lambda_4; \lambda_1\lambda_2} |\mathcal{A}_{\lambda_3\lambda_4; \lambda_1\lambda_2}^{(s)}|^2 \\ &= \frac{1}{16\pi s^2} (4|\mathcal{A}_1^{(t)}|^2 + 4|\mathcal{A}_3^{(t)}|^2 + 8|\mathcal{A}_5^{(t)}|^2). \end{aligned} \quad (11)$$

In the above equations, $\mathcal{A}_i^{(t)}$ ($i=1, 2, 3$) are three of the five independent helicity amplitudes corresponding respectively to $(\lambda_{\bar{2}}\lambda_4; \lambda_1\lambda_{\bar{3}}) = (++, ++)$, $(+-; +-)$, $(++; +-)$. The second equality in Eqs. (10) and (11) is due to crossing symmetry properties of the amplitudes.

It is advantageous to model the form factor H in the LS -basis because in this latter basis the form factor has a well-known $|\mathbf{q}|^L$ threshold behavior that can be explicitly incorporated into the model. The helicity basis is related to the LS -basis by a unitary transformation^[34]. Hence,

$$\sum_{\lambda} |G_{\lambda} H_{\lambda_p\lambda_{\bar{p}}; J_2}(t)|^2 = \sum_{LS} |g_{LS} F_{LS}(t)|^2, \quad (12)$$

where F_{LS} and g_{LS} denote, respectively, the form factor and the coupling constant in the LS basis. For the $\text{pp}\bar{f}_2$ system with $J^{PC} = 2^{++}$, the parity conservation leads to $L=1, 3$ and $S=1$ only. If the form factor is defined in such a way that $F_{LS}(t_r) = 1$, then

$$\Gamma_{\bar{f}_2 \rightarrow \text{p}\bar{\text{p}}} = C_I \frac{M_p^2}{M_{f_2}^2} \frac{|\mathbf{q}_r|}{16\pi^2} (g_{L=1, S=1}^2 + g_{L=3, S=1}^2). \quad (13)$$

Because there is only one value of S , the label S will be dropped but understood in what follows.

It is important to use a form factor which is analytic in both the direct and crossed channels. Liu and Ma proposed the following singularity-free form factor^[31]:

$$(F_L(t))^2 = \left(\frac{t/4 - M_p^2}{t_r/4 - M_p^2} \right)^L \times \left(\frac{e^{t/\lambda_t^2}}{R(-x_t) + e^{t/\lambda_t^2}} \right)^2 \left(\frac{1 + e^{-t/\lambda_s^2}}{R(x_s) + e^{-t/\lambda_s^2}} \right)^2, \quad (14)$$

where the first factor on the r. h. s. is equal to (q^{2L}/q_r^{2L}) . Here, q and q_r are, respectively, the off- and on-shell $\bar{p}p$ relative momentum in the c. m. of the f_2 meson. The F_L has, therefore, the correct threshold q^L -dependence. In Eq. (14), the λ_s , λ_t are the ranges of the form factor, $x_s \equiv (t - 2M_p^2)/\lambda_s^2$, and $x_t \equiv (t - 2M_p^2)/\lambda_t^2$. The function R is defined by

$$R(x) = \frac{1}{2}(1 + \tanh(ax)) = \frac{e^{ax}}{e^{ax} + e^{-ax}} \quad (15)$$

which is analytic and varies rapidly from 0 to 1 when x changes from $\langle 0 \rangle$ to 0, with a controlling the transition speed at $x=0$. With $a > 10$, R will be very close to a step function but does not have the discontinuity of the latter. In fact, R and F_L are infinitely differentiable.

The above analytic properties are absent in the commonly used hadronic form factors in the literature, which are either of an exponential form or of a multiple form. We emphasize that these conventional form factors are unsuitable to analysis involving channel-crossing. For example, the exponential form factor $\exp(t/\Lambda^2)$ is analytic in the s-channel where $t \leq 0$ but diverges in the t-channel where $t > 0$. The multiple form factor $[\Lambda^2/(\Lambda^2 - t)]^n$ ($n = 1, 2, \dots$) has no pole on the real axis of t in the s-channel (where $t \leq 0$) but will have it in the t-channel (where $t > 0$). Conversely, if we use $\exp(-t/\Lambda^2)$ or $[\Lambda^2/(\Lambda^2 + t)]^n$, then the situation will be reversed.

The form factor of Eq. (14) does not have these singularities. In the physical domain of the t-

channel (i. e., $t > 4M_p^2$),

$$(F(t))^2 \propto \frac{q^{2L}}{(e^{t/\lambda_t^2})^2 (1 + e^{-t/\lambda_s^2})^2} \xrightarrow{t \rightarrow +\infty} \frac{t^L}{e^{2t/\lambda_t^2}} \quad (16)$$

which goes to zero, exhibiting the correct energy behavior in the t-channel. We can see that in the t-channel the λ_t controls the form factor. In the s-channel, $t \leq 0$. Hence, $R(-x_t) \simeq 1$ and $R(x_s) \simeq 0$. It follows that

$$(F(t))^2 \propto \frac{q^{2L}}{(1 + e^{t/\lambda_t^2})^2 (e^{-t/\lambda_s^2})^2} \xrightarrow{t \rightarrow +\infty} \frac{t^L}{e^{-2t/\lambda_s^2}}. \quad (17)$$

Hence, λ_s controls the form factor in the s-channel. This singularity-free form factor satisfies the analyticity requirement of the Regge theory and can be used for making analytical continuation between direct and crossed channels. Two remarks are in order. (a) Eq. (6) is given for the sole purpose of making the connection between the t-channel Regge and Feynman amplitudes. It is not needed in fitting the pp scattering data. Hence, the width $\Gamma_{f_2}^{\text{tot}}$ is not an input to the Regge analysis in Ref. [31]. As to the mass M_{f_2} , it enters the analysis through the quantity t_r ($\equiv M_{f_2}^2$) in the form factor, which amounts to a redefinition of the normalization factor and is, therefore, also not an input of dynamics. (b) The important physics inputs are the spin of the meson, J_2 , which determines the values of L in the form factor $F_L(t)$, and the properties of the Pomeron trajectory. Eqs. (4), (7), (10), (11) and (14) were used to fit the pp total and elastic differential cross sections simultaneously. The results are given in Table 1.

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关于软坡密子可能的胶子球本质*

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摘要: 通过把坡密子与观察到的量子数为 $I^G J^{PC} = 0^+ 2^{++}$ 的同位旋张量介子联系起来的思想, 研究了坡密子的胶子内涵。有 4 个由胶子组成的这样的介子都满足坡密子自旋与质量的关系。这些坡密子的候选者可能是混杂态。它们其中之一 $f_2(2 220)$ 介子可能包含着最大的胶子球成分。阐明了实验上还不清楚的关于这个介子宽度的问题, 并给出了它的理论下限。也说明为什么这个介子没有在 $\bar{p}p$ 实验中发现的原因。

关键词: 坡密子; 胶子球; 介子

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